

## Senpai's Last Minute Desperate Notes (Totally Not Copyrighted)

### 1 Physical quantities and units

#### 1.1 Physical quantities

Candidates should be able to:

- 1 understand that all physical quantities consist of a numerical magnitude and a unit
- 2 make reasonable estimates of physical quantities included within the syllabus

- **Physical quantities** consist of a **numerical magnitude** and a **unit**
- Eg. When you are driving, the speedometer shows the speed as 120 km/h. The physical unit here is **speed**, with **120** being the **numerical magnitude** and **km/h** being the **unit**.

#### 1.2 SI units

Candidates should be able to:

- 1 recall the following SI base quantities and their units: mass (kg), length (m), time (s), current (A), temperature (K)
- 2 express derived units as products or quotients of the SI base units and use the derived units for quantities listed in this syllabus as appropriate
- 3 use SI base units to check the homogeneity of physical equations
- 4 recall and use the following prefixes and their symbols to indicate decimal submultiples or multiples of both base and derived units: pico (p), nano (n), micro ( $\mu$ ), milli (m), centi (c), deci (d), kilo (k), mega (M), giga (G), tera (T)

- Note that the units used in the example above is not in **SI**. If we were to convert both the magnitude and units to SI, the speed would then be 33.3 m/s.
- SI unit is a system of measurement that is used and recognized in most countries (except US...)
- SI units can be categorized into two types; **based** and **derived**.
- There are seven base units:

QUANTITY	SI BASE UNIT	SYMBOL
MASS	KILOGRAM	kg
LENGTH	METRE	m
TIME	SECOND	s
CURRENT	AMPERE	A
TEMPERATURE	KELVIN	K
AMOUNT OF SUBSTANCE	MOLE	mol

- Derived units are derived from the seven based units (think of base units as Lego™ blocks and derived units as the castle/ ship/ car/ phone holder you are trying to make)
- Using the eg. above again, **m/s** is a derived SI unit since it is derived from both the base unit for **length** (or distance) (metre) and **time** (seconds).
- Speed is defined by the equation:  

$$\text{speed} = \text{distance} \div \text{time}$$

$$\text{speed} = \text{metres} \div \text{seconds}$$
 Therefore, the SI units for Speed is metres / second ( $\text{ms}^{-1}$ )
- You can use SI base units to check for the homogeneity of an equation.
- What this means is that for an equation, the units on the "left side" of an equal sign must be the same as the units on the "right side"
- Eg. from the kinematics equation  $v = u + gt$   
 $v = \text{m/s}$   
 $u = \text{m/s}$   
 $g = \text{m/s}^2$   
 $t = \text{s}$

"left hand side" =  $v = \text{ms}^{-1}$

"right hand side" =  $u + gt = \text{ms}^{-1} + \text{ms}^{-2} \times \text{s} = \text{ms}^{-1}$

Since "left hand side" = "right hand side" the equation is homogenous

- Some important prefixes can be used to shorten large numbers or units for
- Eg. 100000 metres can be simplified with the prefix **kilo-** to 100 **kilometres** (100 km)
- Some important prefixes are shown below:

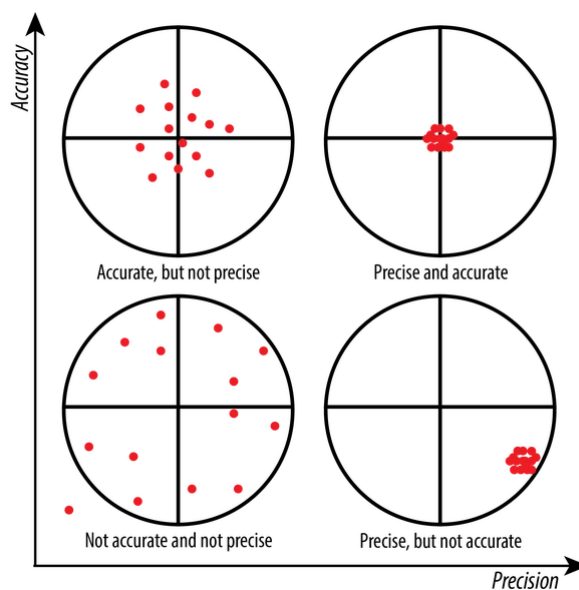
PREFIX	ABBREVIATION	POWER OF TEN
TERA-	T	$10^{12}$
GIGA-	G	$10^9$
MEGA-	M	$10^6$
KILO-	k	$10^3$
CENTI-	c	$10^{-2}$
MILLI-	m	$10^{-3}$
MICRO-	$\mu$	$10^{-6}$
NANO-	n	$10^{-9}$
PICO-	p	$10^{-12}$

### 1.3 Errors and uncertainties

Candidates should be able to:

- 1 understand and explain the effects of systematic errors (including zero errors) and random errors in measurements
- 2 understand the distinction between precision and accuracy
- 3 assess the uncertainty in a derived quantity by simple addition of absolute or percentage uncertainties

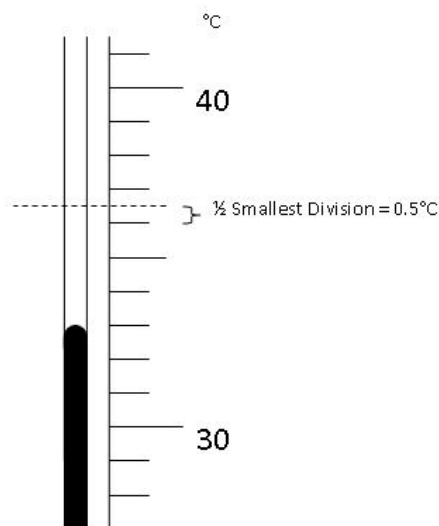
- When measuring anything, it is usually difficult to get accurate results due to there always being a degree of **uncertainty**.
- The cause for this uncertainty is **errors**.
- The two types of common errors are
  - 1) Random errors: Cause by fluctuations in an instrument due to unknown and unpredictable changes in an experiment.  
Eg. electrical noise in the circuit, heat loss due in a solar collector due to wind
  - 2) Systematic errors: From faulty instruments or from wrong techniques used in measurement.  
Eg. when using a weighing scale that doesn't show 0 grams before anything is placed on top.
- An instrument is said to be **accurate** if the values measured is close to the true value.
- An instrument is said to be **precise** if the values measured are close to each other when taking repeated measurements.
- An illustration showing accuracy and precision is shown below:



- **Uncertainty** is the difference between an actual reading and the true value.
- Uncertainty is a range of values around a measurement within which the true value is expected to lie.

- Eg. the true value of the mass of a bottle is 100 g. But when measured on a weighing scale, the reading gives 105 g, the uncertainty can therefore be read as  $\pm 5$  g
- To find uncertainties in different situations:
  - Uncertainty in a reading:**  $\pm$  half the smallest division
  - Uncertainty in a measurement:** at least  $\pm 1$  smallest division
  - Uncertainty in repeated data:** half the range i.e.  $\pm \frac{1}{2}$  (largest - smallest value)
  - Uncertainty in digital readings:**  $\pm$  the last significant digit unless otherwise quoted
- These uncertainties can be represented in a number of ways:
  - Absolute Uncertainty:** where uncertainty is given as a fixed quantity
  - Fractional Uncertainty:** where uncertainty is given as a fraction of the measurement
  - Percentage Uncertainty:** where uncertainty is given as a percentage of the measurement
- Eg.

Example: Liquid in Glass Thermometer



The **absolute uncertainty** would be  $0.5 \times 1^\circ\text{C} = 0.5^\circ\text{C}$

$$T = 33 \pm 0.5^\circ\text{C}$$

The **fractional uncertainty** would be  $0.5/33 = 1/66^\circ\text{C}$

$$T = 33 \pm 1/66^\circ\text{C}$$

The **percentage uncertainty** would be  $1/66 \times 100\% = 1.5\%^\circ\text{C}$

$$T = 33 \pm 1.5\%^\circ\text{C}$$

- Uncertainties can be combined following several rules:
  - When adding / subtracting data – **add the absolute uncertainties**
  - When multiplying / dividing data – **add the fractional uncertainties**
  - When raising to a power – **multiply the absolute certainty by the power**

## 1.4 Scalars and vectors

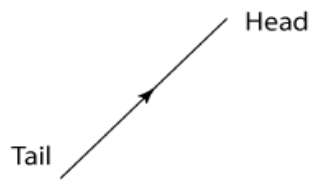
Candidates should be able to:

- 1 understand the difference between scalar and vector quantities and give examples of scalar and vector quantities included in the syllabus
- 2 add and subtract coplanar vectors
- 3 represent a vector as two perpendicular components

- A **scalar** is a quantity which only has a **magnitude**
- Eg. speed, mass, time and distance
- A **vector** is a quantity with both a **magnitude** and **direction**
- Eg. velocity, acceleration, weight, and displacement
- If you want to know if a unit is a scalar or vector try putting a negative in front of it!
- Eg. for eg. you cannot put a minus sign in front of mass because there is no negative mass! (yet)
- In A-levels, you need to know how to combine vectors. You probably already learned this in add maths or SPM physics.

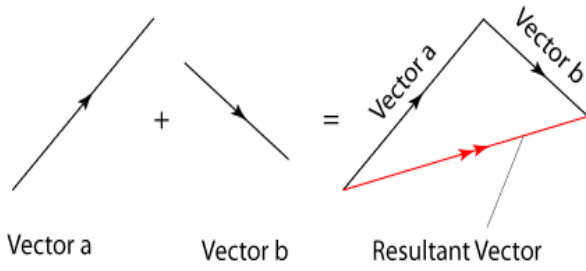
- Here's a refresher:

**Adding vectors**

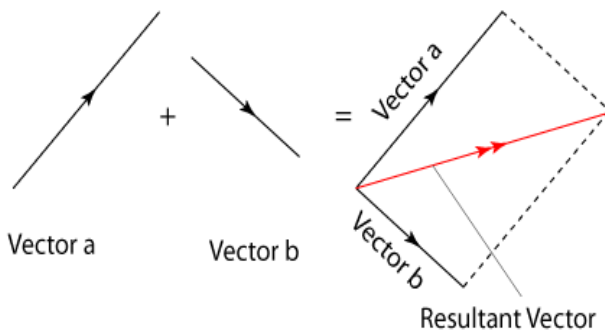


Vector Diagram

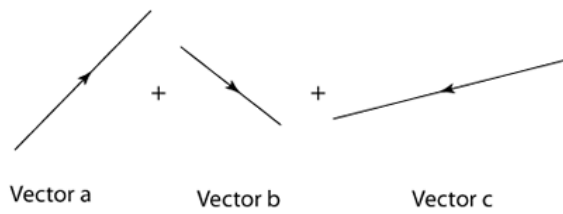
**Triangle Method**



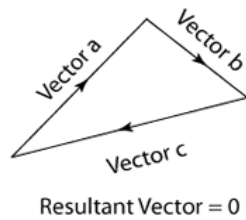
**Parallelogram Method**



**Vectors in equilibrium**



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Resolving vectors in vertical and horizontal components

