

## Chapter 4 Forces, density and pressure

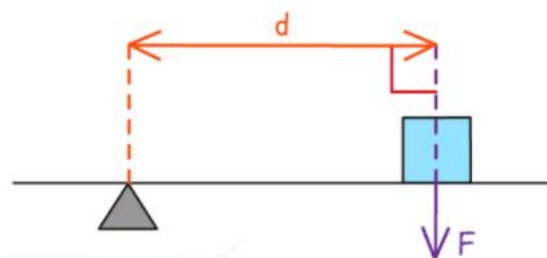
### 4.1 Turning effects of forces

Candidates should be able to:

- 1 understand that the weight of an object may be taken as acting at a single point known as its centre of gravity
- 2 define and apply the moment of a force
- 3 understand that a couple is a pair of forces that acts to produce rotation only
- 4 define and apply the torque of a couple

- The **centre of gravity** of an object is the **point at which the weight of the object may be considered to act**.
- A moment is the **turning effect of a force**
- Think of moments as a force that causes an object to **rotate** instead of moving in a straight line
- The equation for moment is  
Moment = Force x perpendicular distance from the pivot
- The **SI unit** for moment is **Nm**

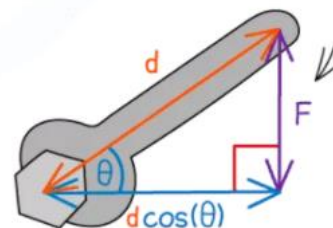
SCENARIO 1:  
PERPENDICULAR  
FORCE



$$\text{MOMENT} = F \times d$$

ALTHOUGH  $d$  IS THE DISTANCE FROM THE PIVOT TO THE FORCE  $F$ , IT IS NOT THE PERPENDICULAR DISTANCE. THEREFORE WE MUST TAKE THE COMPONENT OF THE DISTANCE WHICH IS PERPENDICULAR TO  $F$ .

SCENARIO 2:  
NON-PERPENDICULAR  
FORCE



$$\text{MOMENT} = F \times d \cos(\theta)$$

## 4.2 Equilibrium of forces

Candidates should be able to:

- 1 state and apply the principle of moments
- 2 understand that, when there is no resultant force and no resultant torque, a system is in equilibrium
- 3 use a vector triangle to represent coplanar forces in equilibrium

- The **principle of moment** states that for a system to be **balanced**, the **resultant clockwise must be equal to zero**
- **Clockwise Moment = Counter Clockwise Moment**
- Recall earlier that for a system to be in equilibrium it must satisfy **two criteria**:
  - 1) The resultant force must be equal to zero
  - 2) The resultant moment must be equal to zero

## 4.3 Density and pressure

Candidates should be able to:

- 1 define and use density
- 2 define and use pressure
- 3 derive, from the definitions of pressure and density, the equation for hydrostatic pressure  $\Delta p = \rho g \Delta h$
- 4 use the equation  $\Delta p = \rho g \Delta h$
- 5 understand that the upthrust acting on an object in a fluid is due to a difference in hydrostatic pressure
- 6 calculate the upthrust acting on an object in a fluid using the equation  $F = \rho g V$  (Archimedes' principle)

- **Density** is the **mass per unit volume** of an object

$$\rho = \frac{m}{v}$$

- The **SI unit** for density is **kg/m<sup>3</sup>**
- **Pressure** is defined as **force per unit area**

$$P = \frac{F}{A}$$

- The **SI unit** for pressure is **N/m<sup>2</sup>** or **Pa**
- **Hydrostatic pressure** is the pressure exerted by a fluid at equilibrium at a given point within the fluid, due to the force of gravity
- The magnitude of the pressure depends on the depth (h) the object is submerged in the fluid, the density of the fluid ( $\rho$ ) and the gravitational acceleration (g)

- The equation of hydrostatic pressure is given by

$$p = h\rho g$$

- The derivation is shown below:

Rewrite the pressure formula in terms of  $\rho$ ,  $h$  and  $g$ .

*Hint 1 Write out the "original" pressure formula*

*Hint 2 What is the equation for weight (or force)?*

*Hint 3 Mass is equal to density x volume*

*Hint 4 Volume is equal to area x height of the fluid.*

*Hint 5 Assume both area are the same.*

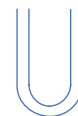
- You can measure pressure by using a manometer  
When both arms are not connected to anything



When one arm is connected to a gas supply and the gas pressure > atmospheric pressure



When one arm is connected to a gas supply and the gas pressure < atmospheric pressure



There are several steps in order to find pressure using a manometer.

**Step 1** Draw equal pressure lines. Remember the pressure is only the same for same fluids.

**Step 2** Draw arrows showing the direction of force caused by the weight of the fluids on the equal pressure lines.

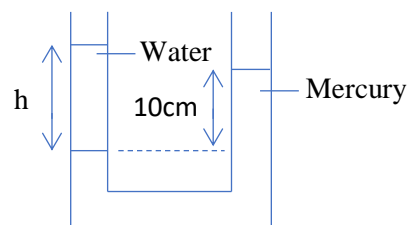
**Step 3** Write the relevant equations down.

**Step 4** Solve the problem

- Don't forget that

**Total pressure = Hydrostatic pressure + Atmospheric pressure (101325 Pa)**

Try the problem below using the steps above:



The manometer consists of water and mercury. You are asked to find  $h$ .

Step 1 Draw equal pressure lines. *Hint: It's obvious this time.*

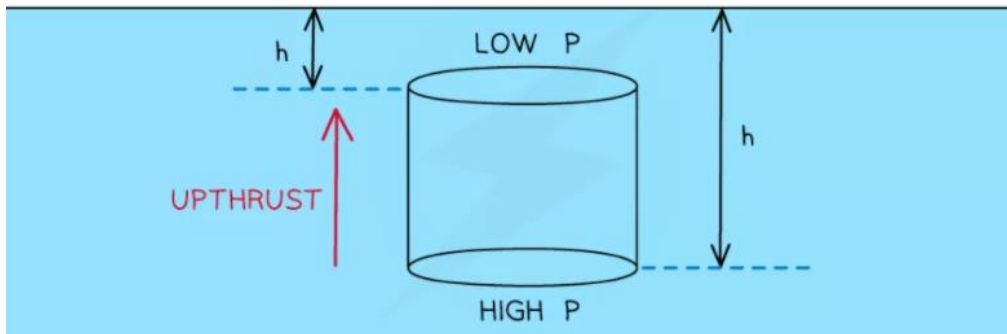
Step 2 Draw arrows showing the direction of force caused by the weight of the fluids

*Hint: Both arms are exposed to the atmosphere*

Step 3 Write the relevant equations down. *Hint:  $P = \rho g h$*

Step 4 Solve the problem

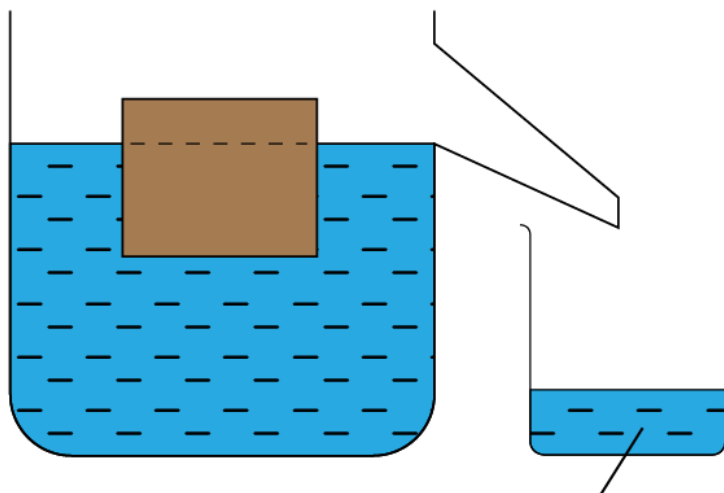
- Upthrust is a force which pushes upwards on an object submerged in a fluid
- Think boat or submarine
- Another name for upthrust is buoyancy force
- Buoyancy is caused by the difference in hydrostatic pressure at the top and bottom of a submerged vessel



- Archimedes' principle states that an object submerged in a fluid at rest has an upthrust equal to the weight of the fluid displaced by the object.

$$F = \rho g V$$

- An example is shown below



Weight of displaced water  
= 20N