

2 Kinematics

2.1 Equations of motion

Candidates should be able to:

- 1 define and use distance, displacement, speed, velocity and acceleration
- 2 use graphical methods to represent distance, displacement, speed, velocity and acceleration
- 3 determine displacement from the area under a velocity–time graph
- 4 determine velocity using the gradient of a displacement–time graph
- 5 determine acceleration using the gradient of a velocity–time graph
- 6 derive, from the definitions of velocity and acceleration, equations that represent uniformly accelerated motion in a straight line
- 7 solve problems using equations that represent uniformly accelerated motion in a straight line, including the motion of bodies falling in a uniform gravitational field without air resistance
- 8 describe an experiment to determine the acceleration of free fall using a falling object
- 9 describe and explain motion due to a uniform velocity in one direction and a uniform acceleration in a perpendicular direction

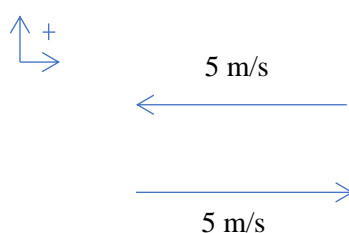
- **Speed** is the total **distance** travelled per unit time (ms^{-1})
- Since **distance** is a **scalar**, **speed** is a scalar
- **Velocity** is the rate of change of **displacement** of an object (ms^{-1})
- Since **displacement** is a **vector**, **velocity** is a vector

$$v = \frac{s}{t}$$

v is the speed, s is the displacement and t is the time taken

Note: In velocity the positive/ negative sign indicates direction.

- Example



Speed of top arrow: 5 ms^{-1}

Velocity of top arrow: -5 ms^{-1}

Speed of bottom arrow: 5 ms^{-1}

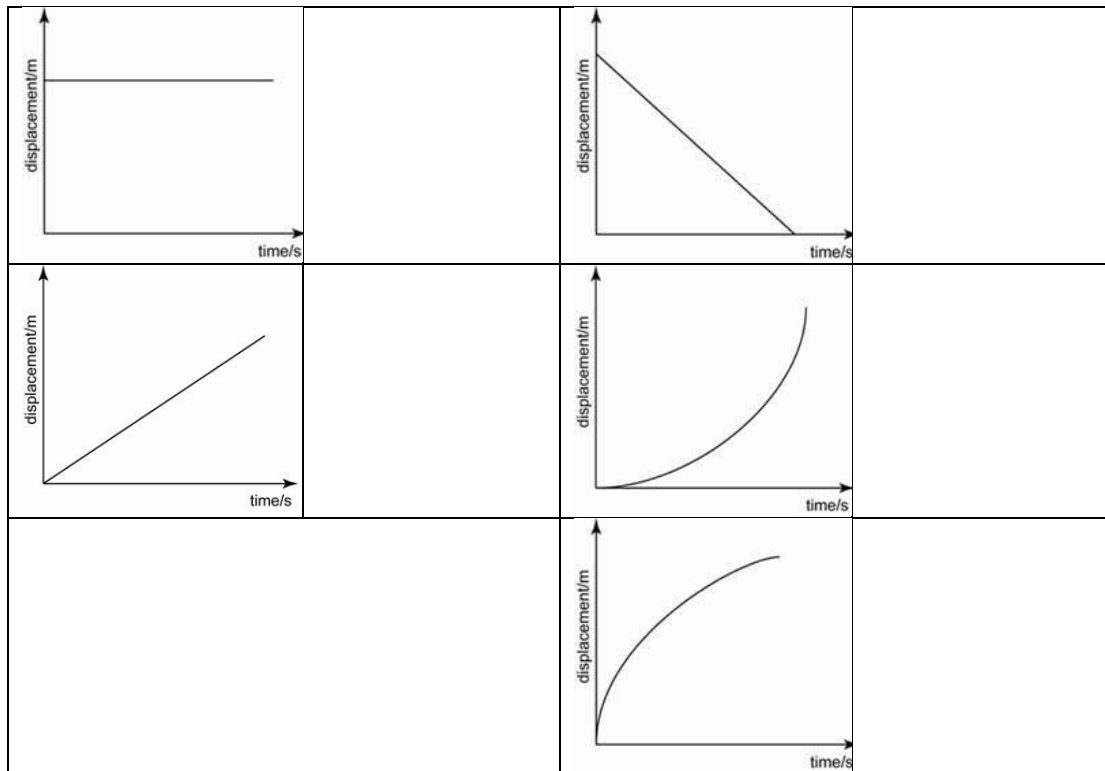
Velocity of bottom arrow: 5 ms^{-1}

- **Acceleration** is the rate of change of **velocity** of an object (ms^{-2})
- **Acceleration** is a **vector**.

$$a = \frac{v - u}{t}$$

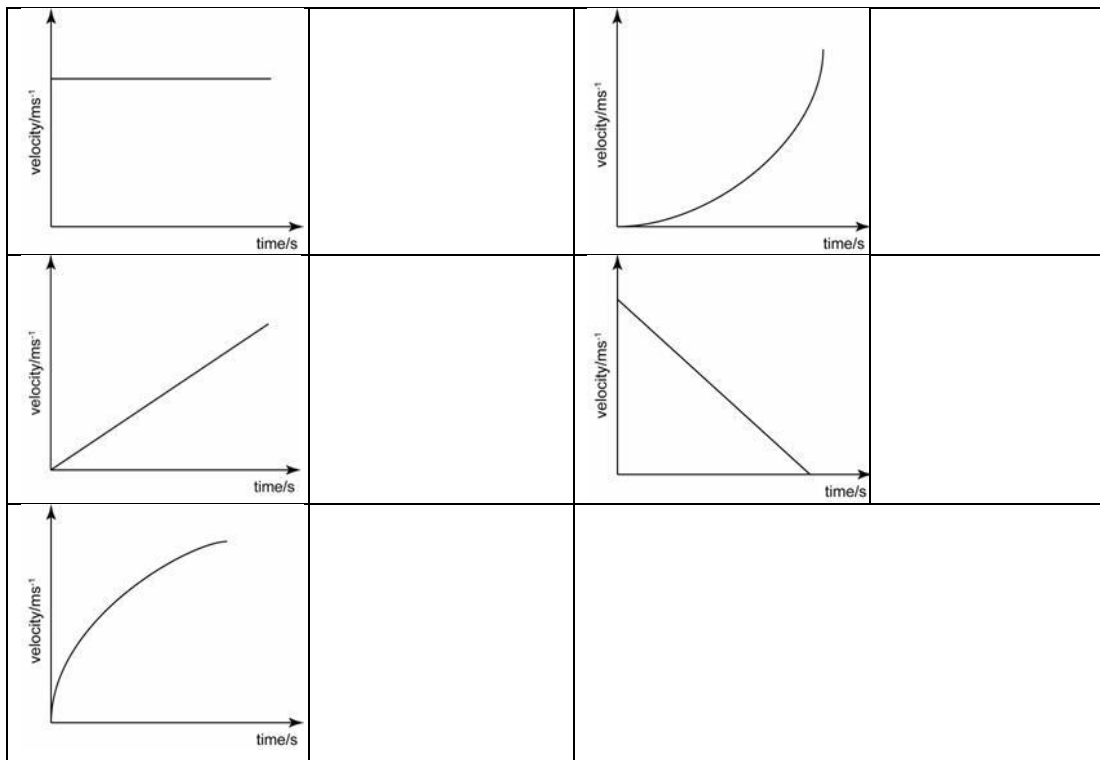
- There are **three** types of motion graphs to represent displacement, velocity and acceleration.
- The three graphs are **displacement-time graphs, velocity-time graphs and acceleration-time graphs**
- You most likely learned the first two graphs in IGCSE or SPM

Displacement-time graphs



- **slope equals velocity**
- the **y-intercept** equals the **initial displacement**
- a **straight** line represents a **constant** velocity
- a **curved** line represents an **acceleration**
- a **positive slope** represents motion in the **positive direction**
- a **negative slope** represents motion in the **negative direction**
- a **zero slope** (horizontal line) represents a state of **rest**
- the area under the curve is meaningless

Velocity-time graphs



- **slope equals acceleration**
- the **y-intercept** equals the **initial velocity**
- a **straight** line represents **uniform** acceleration
- a **curved** line represents **non-uniform** acceleration
- a **positive** slope represents an **increase** in **velocity** in the **positive** direction
- a **negative** slope represents an **increase** in **velocity** in the **negative** direction
- a **zero** slope (horizontal line) represents motion with **constant** velocity
- the **area** under the curve equals the **change** in **displacement**

• On an **acceleration-time** graph...

- slope is meaningless
- the y-intercept equals the initial acceleration
- a zero slope (horizontal line) represents an object undergoing constant acceleration
- the area under the curve equals the change in velocity

- **Kinematic equations** of motion are a set of **four** equations which can describe any objects moving with **constant acceleration**
- The four equations are:

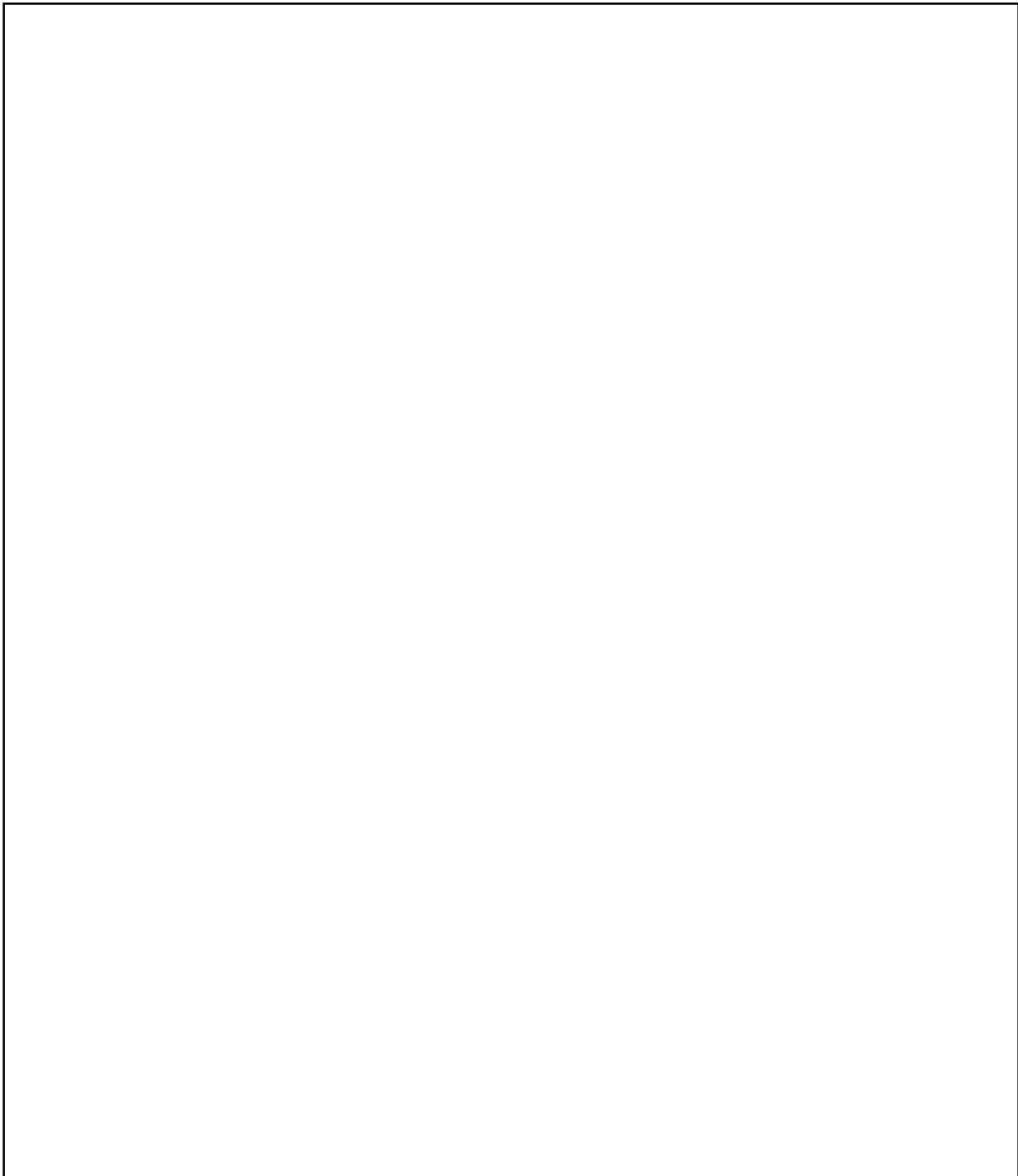
$$v = u + at$$

$$d = 0.5(v+u)t$$

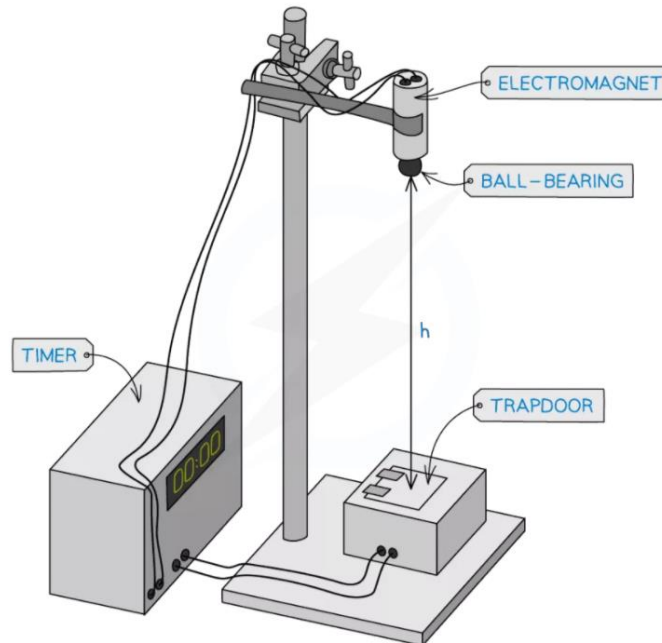
$$d = ut + 0.5at^2$$

$$v^2 = u^2 + 2ad$$

For A-levels you must know how they are derived



- Below is a description of an experiment to determine acceleration of free fall using a falling object
- **Apparatus**
Metre rule, ball bearing, electromagnet, electronic timer, trapdoor



- **Method**
When the current to the magnet switches off, the ball drops and the timer starts.
When the ball hits the trapdoor, the timer stops.
The reading on the timer indicates the time it takes for the ball to fall a distance, h .
This procedure is repeated several times for different values of h , in order to reduce random error.
The distance, h , can be measured using a metre rule as it would be preferable to use for distances between 20 cm - 1 m.
- **Analysing data**
The known quantities are
Displacement $s = h$
Time taken = t
Initial velocity $u = 0$
Acceleration $a = g$
The equation that links these quantities is
$$s = ut + \frac{1}{2} at^2$$
$$h = \frac{1}{2} gt^2$$
Using this equation, deduce g from the gradient of the graph of h against t^2

- Sources of error

Systematic error: residue magnetism after the electromagnet is switched off may cause the time to be recorded as longer than it should be

Random error: large uncertainty in distance from using a metre rule with a precision of 1mm, or from parallax error

- For A-levels it is not sufficient to know about motion only in 1 dimension. The candidate must be able to solve motion in 2 dimensions as well.

- An object undergoing projectile motion consists of 2 components; **vertical and horizontal**.

- The key terms in solving projectile motion problems are

Time of flight: how long the projectile is in the air

Maximum height attained: The height at which the projectile is momentarily at rest

Range: The horizontal distance travelled by the projectile

- From the diagram below, it can be inferred that to attain maximum **range**, the optimal angle of flight is **45°**.

